## multi-step inequalities

Review: Solve the inequality and number line, and then explain the solution.
$-4 p+28>8$

## using the distributive property

When we distribute, $\qquad$ the outside number by BOTH terms inside the parentheses!

1) $4(1-2 t)>28$
2) $36 \geq 4(2 m+10)$

## . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . multi-step Inequalities

***Remember: You are always using the same steps as solving an $\qquad$ .

But you must $\qquad$ the inequality sign when multiplying or dividing by a $\qquad$ !

Step 1: Draw a $\qquad$ down from the $\qquad$ .

Step 2: $\qquad$ if needed.

Step 3: Combine $\qquad$ .

Step 4: $\qquad$ the variable.

Step 5: Undo any $\qquad$ or $\qquad$ .

Step 6: Undo any $\qquad$ or $\qquad$ .

Step 7: $\qquad$ each step.

Try-it!! Solve, graph and then explain the solution.
3) $2 t+4-3 t \geq-1$
4) $4(w-2)-w \leq-10$
5) $4(1+2 t)>28$
6) $24>3(x+2)$
7) $2 n-3(n+3) \leq 14$
8) $3 s+16-4 s<7$

## Inequalities with Varriables on Both Sides

Review: Fill in the blanks.

## Steps for Variables on Both Sides:

Step 1: Draw a $\qquad$ down from the inequality sign to separate the two sides.

Step 2: $\qquad$ if needed.

Step 3: Combine $\qquad$
$\qquad$ on each side separately if needed.

Step 4: $\qquad$ the terms with the variable.

Step 5: Move the $\qquad$ variable to the other side by doing the $\qquad$ .

Step 6: Undo any $\qquad$ or $\qquad$ -

Step 7: Undo any $\qquad$ or $\qquad$ .

Step 8: $\qquad$ each step.


1) $6 z-15<4 z+11$
2) $-3(v-3) \geq 5-4 v$
3) $2 m-3<4 m+5$

Try-it!!! Solve and Graph the number line
4) $3 w+2<2 w+5$
5) $3 x+2>-4 x+16$
6) $3(-4+m) \geq 8 m-28$
7) $3(q+2) \leq-5 q-10$

## Inequalities with Decimals \& Fractions

Review: Solve the following, number line and then explain the solution:

$$
r+3>5 r+19
$$

When an inequality has $\qquad$ and $\qquad$ not much changes!


Convert all fractions to decimals first if you can.
L_- - - - - - - - -
If a fraction is attached to your variable (and it can't be converted to a decimal), $\qquad$ both sides of the inequality by the $\qquad$ to get rid of it. $\qquad$ !)

Solve the following inequalities, number line and explain.

1) $5 \frac{1}{2} \leq \frac{1}{4} x+5$
2) $0.02 y+200<0.03 y+350$
3) $\frac{5}{6} \leq \frac{2}{3} x+\frac{1}{2}$

## TRY IT!!!!

4) $0.02 x+0.7 \geq 0.8$
5) $0.35 x+0.6 \leq 0.1 x+1$
6) $2(x-3)>1.2-x$
7) $\frac{1}{16} x+\frac{1}{4}<\frac{1}{2}$

Solve the inequality and number line the solution. Then DESCRIBE the solution set.

1. $t-12 \geq 8$
2. $4 k<24$

3. $16 \leq h+9$

4. $\frac{a}{-5}>2$

5. $12 \geq-4 x-4$

6. $2 m+6 \leq 16$

7. $-5 a-10 \geq 20$

8. $-\frac{x}{4}+2<3$

9. $8(1+2 x)<32$

10. $6 x+2 \leq 2 x+6$

11. $0.3 w+4.2>7.3+3.9 w$

12. $\frac{1}{7} x-8>-12$



## Exercise 1

Determine whether each claim given below is true or false.
a. Right now, I am in math class and English class.
b. Right now, I am in math class or English class.
c. $3+5=8$ and $5<7-1$.
d. $\quad 10+2 \neq 12$ and $8-3>0$.

These are all examples of declarative compound sentences.
e. When the two declarations in the sentences above were separated by "and," what had to be true to make the statement true?
f. When the two declarations in the sentences above were separated by "or," what had to be true to make the statement true?

## Example 1

Solve each system of equations. Then number line the solution
a. $x+8=3$ or $x-6=2$
b. $4 x-9=0$ or $3 x+5=2$
c. $x-6=1$ and $x+2=9$
d. $3 x+2=8$ and $-4 x-2=-10$
e. $5 x-8=-23$ or $x+1=-10$
f. $x-9=0$ or $x+15=0$

Name:

## Determine if each sentence is true or false. Explain your reasoning.

a. $8+6 \leq 14$ and $\frac{1}{3}<\frac{1}{2}$.
b. $5-8<0$ or $10+13 \neq 23$
1.)
a. Using a colored pen, pencil or highlighter, graph the inequality $x<3$ on the number line below.

b. Using a different colored pencil, graph the inequality $x>-1$ on the number line below.

c. Using a third colored pencil, darken the section of the number line where $x<3$ and $x>-1$.

2.) Write a compound inequality for each graph.
a.

b.

C. Rewrite as a compound sentence and graph the sentence on a number line.
$1 \leq x \leq 3$


Solve the compound inequality and graph the solution(s) to each of the following on a number line.
3.) $x<9$ and $x>7$
4.) $-10<\mathrm{p}+2<2$


Try It! Solve each compound inequality. Graph its solution set.
5.) $y+4>1$ and $y+2<1$

6.) $-8<h+2<2$


## COMPOUND -OR-INEQUALITIES

## Determine if the following are true or false.

a. $3<5+4$ or $6+4=9$.
b. $\quad 16-20>1$ or $5.5+4.5=11$

## Exercise 1

a. Using a colored pencil, graph the inequality $x<-4$ on the number line below.

b. Using a different colored pencil, graph the inequality $x>0$ on the number line below.

c. Using a third colored pencil, darken the section of the number line where $x<-4$ or $x>0$.


Example 2: Write a compound inequality for each graph.

b.


Example 3: Graph each compound sentence on a number line.
a. $x \leq-5$ or $x \geq 2$
b. $x+4<2$ or $x-2>1$

c. $3 c+4 \geq 13$ or $6 c-1<11$
d. $\quad 12+b \geq 16$ or $b+9<11$


## COMPOUND INEEOALIIIIES VIIH NO SOLUTION Review:

Solve the compound inequality, graph on a number line, and write describe the solution: $-10<x+2 \leq-1$


## 

When we graph compound inequalities separated by $A N D$, our solution is where the inequalities $\qquad$ .

If we graph a compound inequality separated by $A N D$, and the inequalities do not
$\qquad$ then there is $\qquad$ .

## Name a number that is in the solution:

$$
x \geq 3 \text { and } x<7
$$

$$
x>5 \text { and } x<2
$$

Solve the following inequalities, graph on a number line, and describe the solution:

1. $7-3 x<16$ and $x+12<-8$

2. $8 \leq 2(x-3)<4$
3. $\frac{p}{2}<5$ and $\frac{p}{3} \geq 4$

## Compound Inequalities Review

Solve and then graph the solution set.

| 1. $n-10 \geq 0$ or $-5+n<-6$ | 2. $x+1 \geq 3$ or $x+6<4$ |
| :---: | :---: |
| 3. $\frac{v}{2} \leq 0$ and $v-2>-10$ | 4. $28<9 k+1<55$ |


| 5. $6 y>-36$ or $-3 y \geq 24$ | 6. $b+7<11$ or $9+b \geq 16$ |
| :---: | :---: |
| 7. $2<2 t<10$ | 8. $7+m \geq 2$ and $m+1<2$ |

Write a compound inequality for each solution set shown below.
1.


Solve the compound inequality and graph its solution.
2. $b-2>18$ or $3 b<54$
3. $3 j \geq 6$ or $3 j \leq-6$
4. $7+2 a>9$ or $-4 a>8$
5. $6 x>-36$ or $3 x \leq-24$

Name $\qquad$

## Solving a compound "AND" inequality

1) $m+2>2$ and $m-4<2$
2) $-5<k+3 \leq 3$
3. $2 a+7<9$ and $a+5>2$

4. $-4 b>8$ and $2 b>-6$

Solve the following compound equations and number line the solution.
1.) $-2 x-3=-9$ or $5 x-7=13$
2.) $3 x-6=12$ and $4 x+2=26$
3.) $-7 x+2=16$ and $3 x-5=-11$
4.) $6 x-1=5$ or $-2 x-3=7$

Solve the following inequalities. Number line and EXPLAIN the solution.

1. $2(m+3) \leq 16$
2. $8 n-10<6-2 n$
3. $6 t+12>8+8 t$

4. $3(d-2)>16+2 d$


Solve the following inequalities. Then number line and EXPLAIN the solution.
1.) $0.6 m+3 \leq 2 m+0.2$
3.) $\frac{3}{5}(x+2) \leq x-4$
2.) $0.6(n+10)>3.6$
4.) $\frac{1}{2} w+7 \geq 2 w-2$

Name:
Solve the inequality and graph its solution. Then describe the solution.

1. $5+4 x \geq x+8$
2. $3 z+7<2 z+10$

3. $12+4 m \geq 8 m-8$
4. $3(x-2)-2 x>4 x+9$

Solve the following inequalities. Then number the line and EXPLAIN the solution.

1) $3(d+2)>6$
2) $26 \geq 2(m+10)$

3) $18>2 m+6-5 m$
4) $2(b-3)-4 b \geq 4$

