

# Foundations of Math

## Chapter 6 Packet

Name:

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# INTRO TO FUNCTIONS

**Examples of Functions:**

$\{(2, 5), (5, 2), (0, 0)\}$

$\{(-8, -3), (-3, -8), (7, 7)\}$

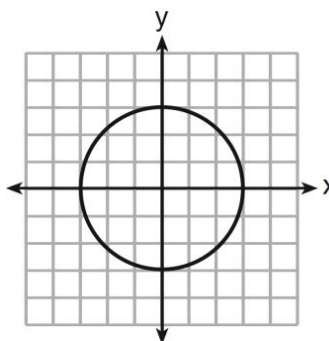
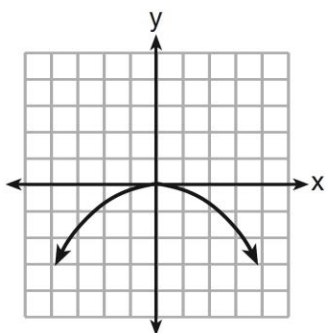
**Examples that are NOT Functions:**

$\{(2, 5), (5, -9), (2, 0)\}$

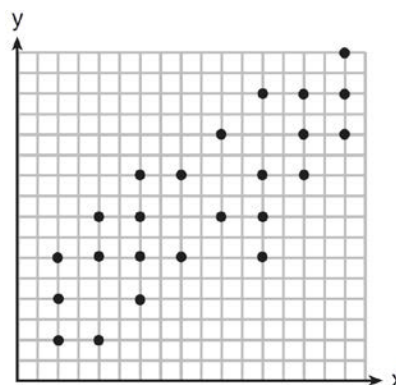
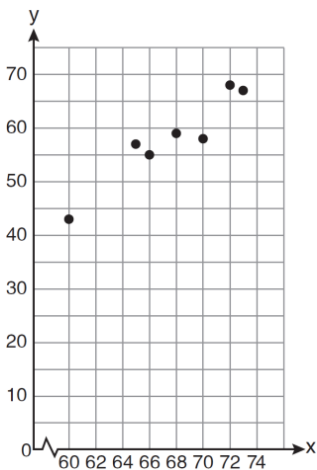
$\{-8, -3, -5, 7\}$

$x$	-2	0	1	2
$y$	0	-2	-3	-4

$x$	3	3	2	0
$y$	1	4	5	-3



Functions pass the \_\_\_\_\_ which is when a graph does not \_\_\_\_\_ the vertical line more than \_\_\_\_\_.



In your own words, define "function".

Domain:

Range:



**Ex 1) Let  $x = \{1, 2, 7, 4\}$  and  $y = \{5, 6, 7, 8, 9\}$ .  $f$  and  $g$  are defined below.**

$$f(x) = \{(1, 7), (2, 5), (7, 6), (4, 7)\} \quad g(x) = \{(1, 5), (2, 6), (1, 8), (2, 9), (7, 7)\}$$

a) Is  $f$  a function? If yes, what is the domain and range? If no, explain why.

b) Is  $g$  a function? If yes, what is the domain and range? If no, explain why.

c) What is  $f(2)$ ?

d) If  $f(x) = 7$ , then what is  $x$ ?

# EVALUATING FUNCTIONS-DAY I

Review: Determine if the following are functions. If they are, find the domain and the range.

1.)  $\{(2, 3), (4, 0), (-2, 3), (5, 1)\}$

2.)  $\{(3, -1), (4, 6), (7, 2), (3, 6)\}$

Evaluating: Just \_\_\_\_\_ and \_\_\_\_\_!

1. Find the value of each function for the given input.

Let  $f(x) = 6x - 3$ ,

let  $g(x) = 0.5(4)^x$ , and

let  $h(x) = x^2 - 3x + 4$ .

a.  $f(0)$

e.  $g(0)$

i.  $h(2)$

b.  $f(-10)$

f.  $g(-1)$

j.  $h(-2)$

c.  $f(2)$

g.  $g(2)$

k.  $h(-4)$

d.  $f\left(-\frac{2}{3}\right)$

h.  $g\left(\frac{1}{2}\right)$

l.  $h\left(\frac{2}{3}\right)$

Let  $f(x) = 6x - 3$  and let  $h(x) = x^2 - 3x + 4$ .

m.  $f(1) + f(2)$

n.  $h(2) + h(1)$

2. Since a variable is a placeholder, we can substitute letters that stand for numbers in for  $x$ . Let  $f(x) = 6x - 3$ , and let  $g(x) = 0.5(4)^x$ , and suppose  $a, b, c$ , and  $h$  are real numbers. Evaluate each function for the given input.

a.  $f(a)$

c.  $g(b)$

b.  $f(2a)$

d.  $g(3b)$

Name: \_\_\_\_\_

Notes #63

# Evaluating Functions Day 2

Review: Evaluate the following:

$$f(x) = -4x + 5 \text{ and}$$

$$g(x) = 2(16)^x$$

1.)  $f(-3)$

2.)  $g\left(\frac{1}{2}\right)$

3.)  $g(0)$

Since a variable is a placeholder, we can substitute letters that stand for numbers in for  $x$ . Let  $f(x) = 6x - 3$ , and let  $g(x) = 0.5(4)^x$ , and suppose  $a$ ,  $b$ ,  $c$ , and  $h$  are real numbers. Evaluate each function for the given input.

a. $f(a) + f(h)$	b. $g(b - 3)$
c. $f(a + h)$	d. $g(b + c)$

e. $f(a + 1) - f(a)$	f. $f(a + h) - f(a)$
g. $f(2 + h) - f(h)$	h. $g(b + 1) - g(b)$

Let  $m(x) = 5x + 10$  and  $k(x) = -4x$ . Evaluate.

i.  $m(2) - k(12)$

j.  $m(-7) + k(-2)$



# Domain and Range

**Review:**

What is Domain:

What is Range:

Find the domain and range of the following:  $\{(2, 5), (4, 2), (8, -3), (11, 1)\}$

1) Provide a suitable domain and range to complete the definition of each function.

a. Let  $f(x) = 2x + 3$ .

b. Let  $C(x) = 9x + 130$ , where  $C(x)$  is the number of calories in a sandwich containing  $x$  grams of fat.

c. Let  $B(x) = 100(2)^x$ , where  $B(x)$  is the number of bacteria at time  $x$  hours over the course of one day.

2) Donovan purchased a bag of Flamin' Hot Cheetos. The nutrition on the box stated that a serving of 10 cheetos contains a total of 100 calories. A full bag of Flamin' Hot Cheetos contains 170 calories. What is the domain and the range for the bag?

3) A local DJ business charges \$70 per hour plus a \$1200 equipment fee. Find the domain and range over a 5 hour period.

4) A local DJ business charges charges \$280 dollars per hour. Find the domain and range over a 5 hour period.

# interval notation

Symbol	Meaning
( (Parentheses)	• • • •
[ [Bracket]	• • • •

$3 < x < 10$	As an inequality
	In Interval Notation
←————→	

	As an inequality
$(3,10]$	In Interval Notation
←————→	

	As an inequality
$[3,10)$	In Interval Notation
←————→	

$3 \leq x \leq 10$	As an inequality
	In Interval Notation
←————→	

- Which interval notation represents the set of all numbers from 2 through 7, inclusive?
  - $(2,7]$
  - $(2,7)$
  - $[2,7)$
  - $[2,7]$
- Which interval notation represents the set of all numbers greater than or equal to 5 and less than 12?
  - $[5,12)$
  - $(5,12]$
  - $(5,12)$
  - $[5,12]$

## infinity:

Infinity is not a \_\_\_\_\_, it is an \_\_\_\_\_.

It represents something with \_\_\_\_\_.

We use the symbol:

$x \leq 3$       ←————→

\_\_\_\_\_

$x > 17$       ←————→

\_\_\_\_\_

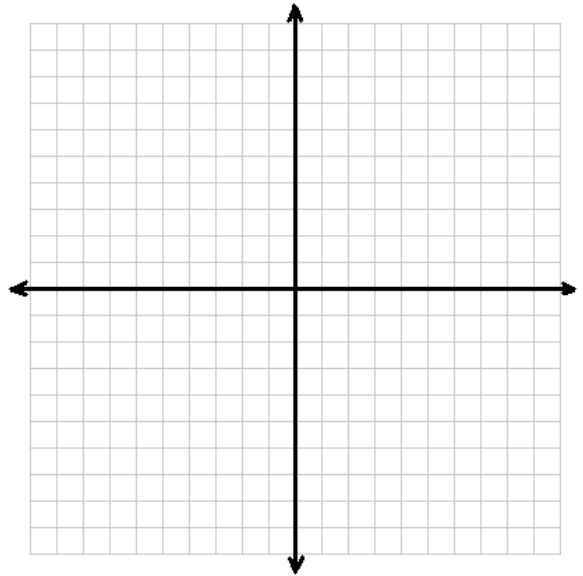
- 3) In interval notation, the set of all real numbers greater than -4 and less than or equal to 11 is represented by:
- 4) Give the interval notation that represents the set of all real numbers greater than 2 and less than or equal to 20?
- 5) The inequality  $-2 \leq x < 4$  can be written as:
- 6) Which interval notation represents  $-3 \leq x \leq 3$
- 7) Which set of integers is included in  $(-1, 3)$ ?
- 8) Which set of integers is included in  $[-5, 0]$ ?
- 9) Which set of integers is included in  $(1, 7)$ ?
- 10) Which set of integers is included in  $[14, 25)$ ?
- 11) Give the interval notation that represents the set of all numbers from -4 through 8, exclusive.

Name: \_\_\_\_\_

# Graphing Linear Functions on an Interval

Sketch the graph of the following equation:

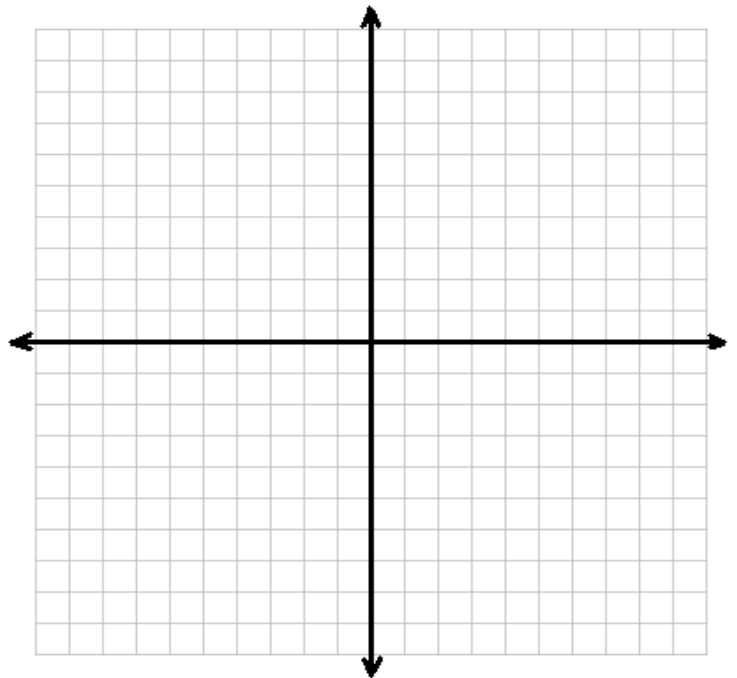
$$f(x) = 2x - 3$$



What if we use interval notation?

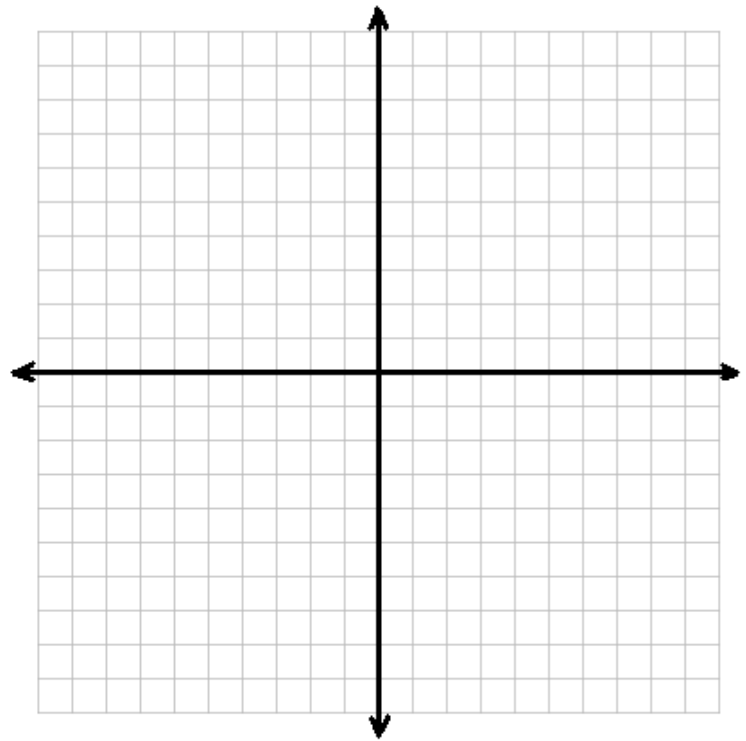
1)  $f(x) = 2x - 3; [-1, 4]$

$x$		$f(x)$



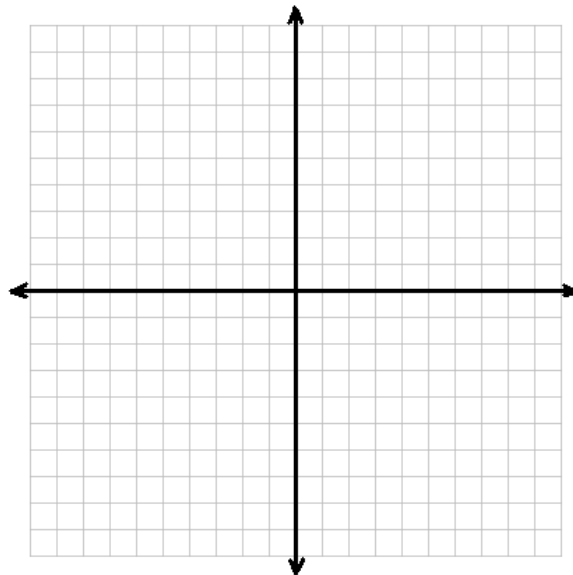
2)  $f(x) = \frac{1}{2}x - 2; (-3, 3)$

$x$		$f(x)$



3)  $f(x) = -3x + 5; (-1, 5]$

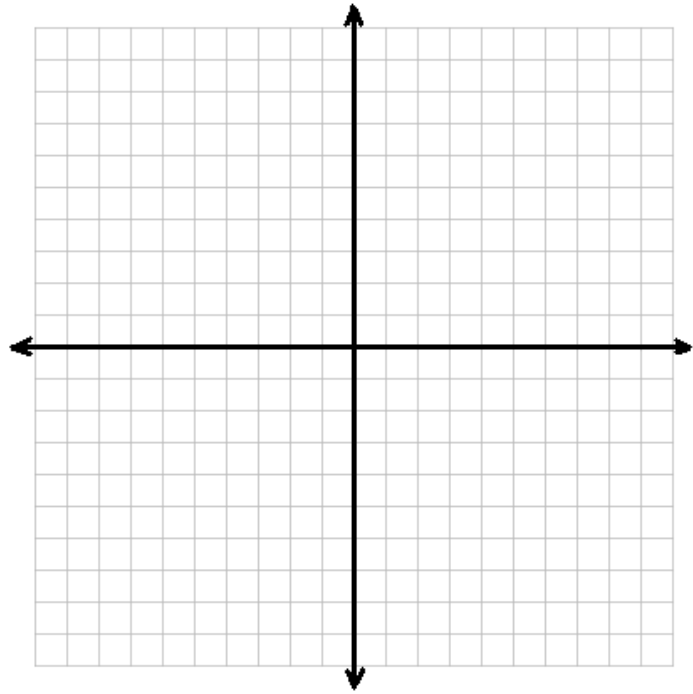
$x$	$f(x)$



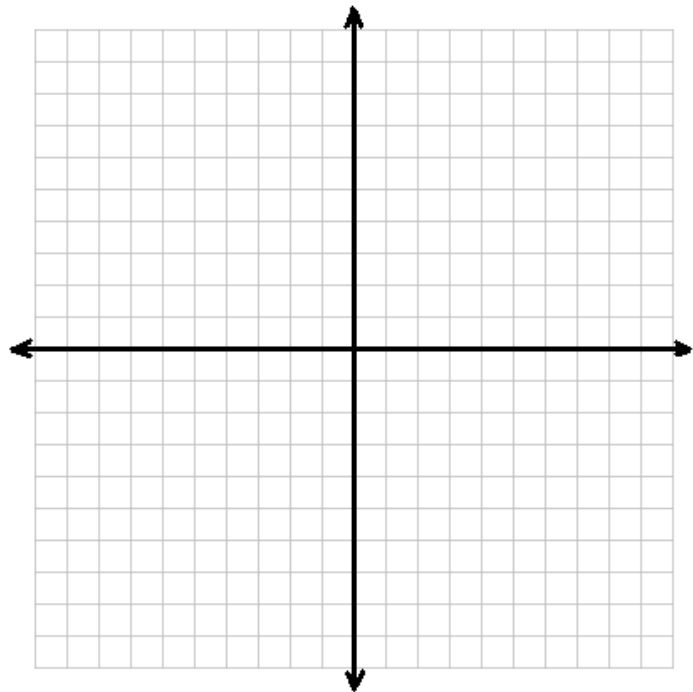
### Getting Coordinates with a Calculator

- Step 1: Press **Y=**
- Step 2: Type in function
- Step 3: Press **2<sup>nd</sup>**, press **Graph**
- Step 4: Use the arrows to find your x values.
- Step 5: Write them in a table on your paper

4)  $f(x) = 3x - 2; [-2,4]$



5)  $f(x) = -\frac{1}{2}x + 2; [-3,1)$







# Graphing Exponential Functions on an Interval

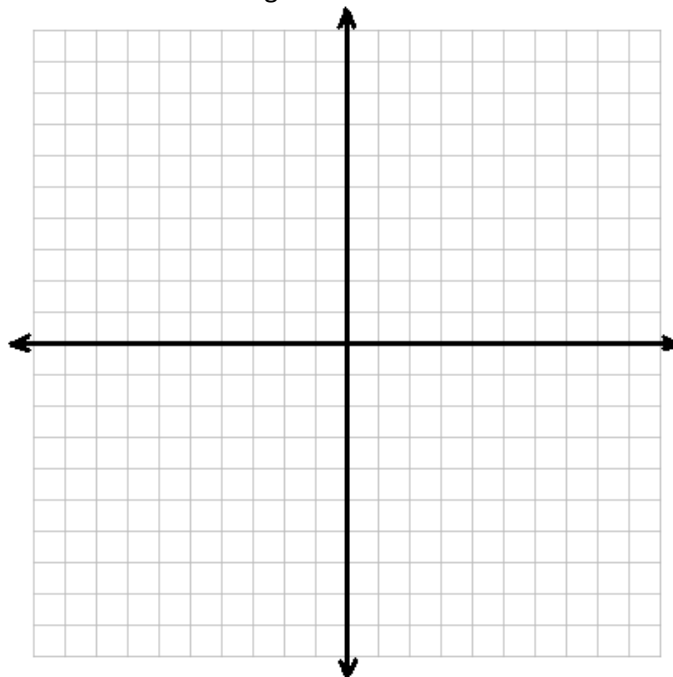
Yesterday we graphed \_\_\_\_\_ functions.

We can graph different types of functions in a given interval too.

Exponential functions have the \_\_\_\_\_ in the \_\_\_\_\_.

- 1) Sketch the graph of the following equation and find the domain and range:

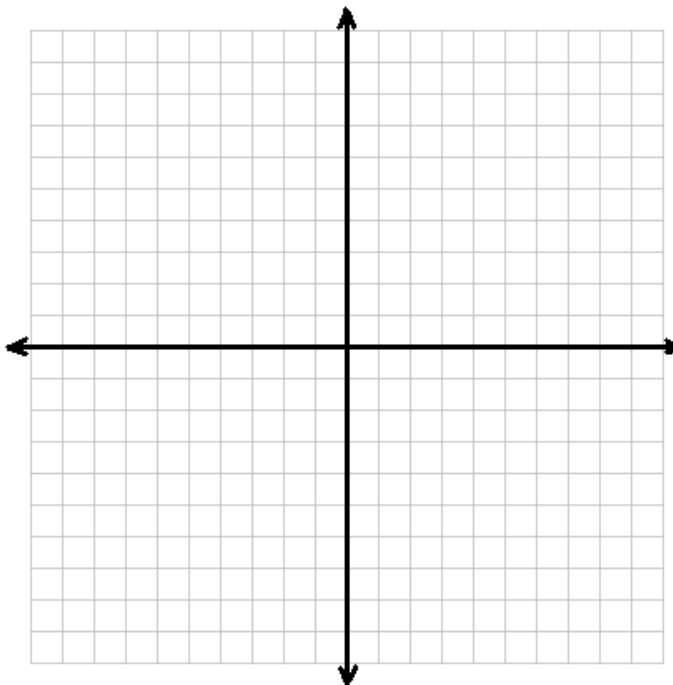
$$f(x) = 2^x ; [-1, 3]$$



Domain: \_\_\_\_\_

Range: \_\_\_\_\_

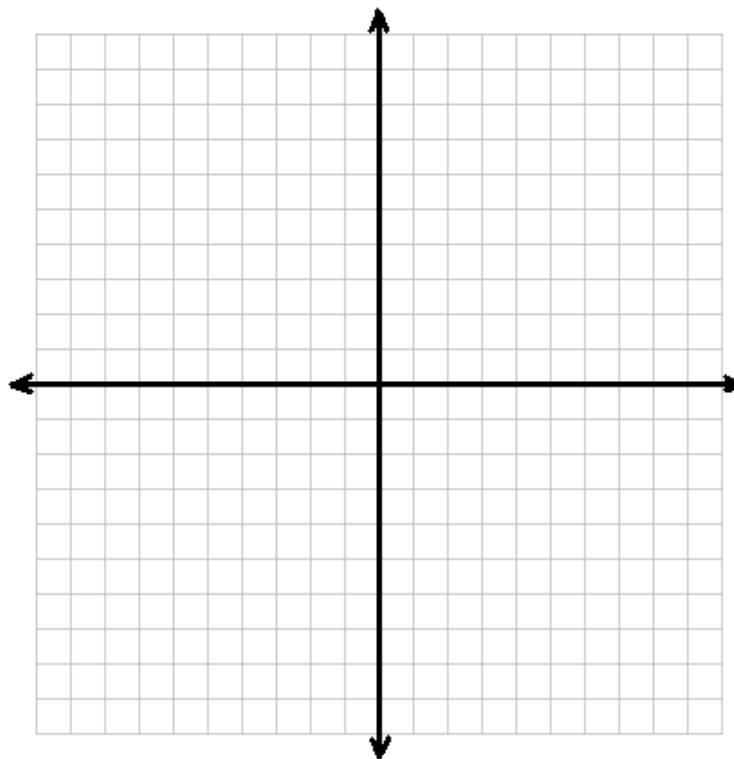
- 2)  $f(x) = \left(\frac{1}{2}\right)^x ; (-2, 2)$



Domain: \_\_\_\_\_

Range: \_\_\_\_\_

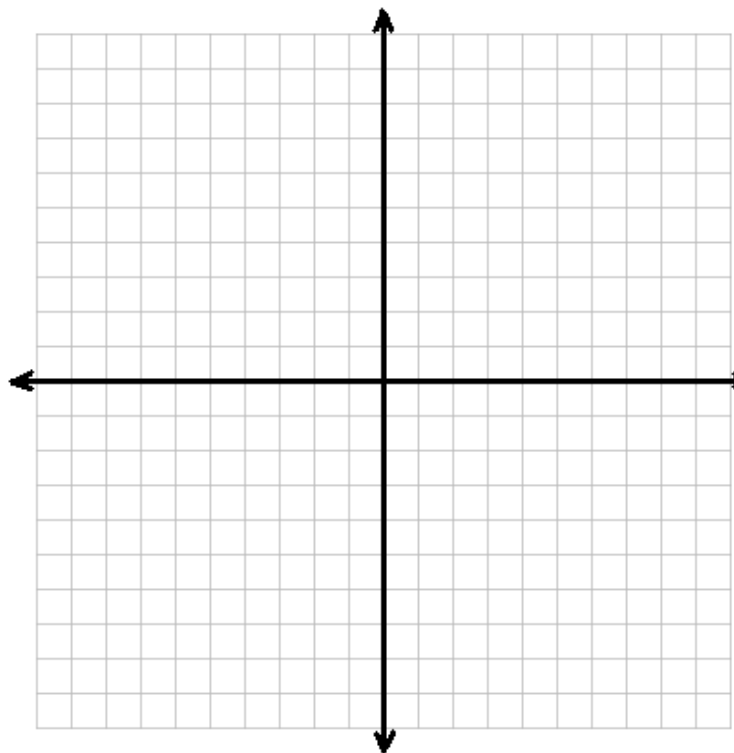
3)  $f(x) = \left(\frac{1}{3}\right)^x$  ;  $[-2, 1)$



Domain: \_\_\_\_\_

Range: \_\_\_\_\_

4)  $f(x) = 2.5(2)^x$  ;  $(-1, 2]$



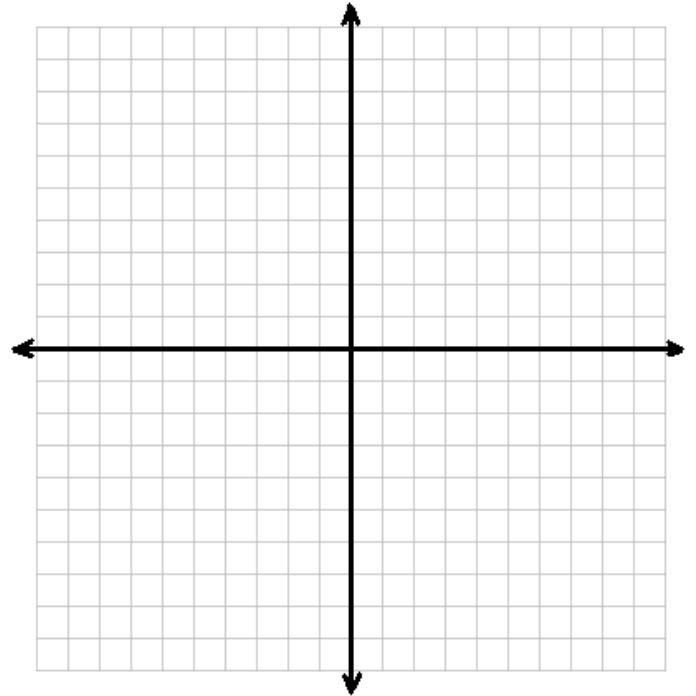
Domain: \_\_\_\_\_

Range: \_\_\_\_\_

Name: \_\_\_\_\_

Sketch the graph of the following equation and find the domain and range:

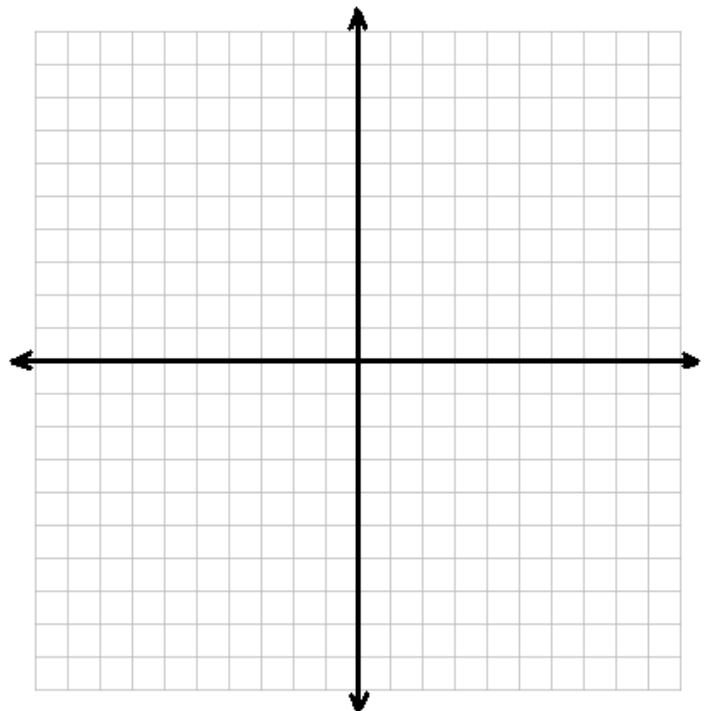
1.)  $f(x) = 2(2)^x ; [-1, 2]$



Domain: \_\_\_\_\_

Range: \_\_\_\_\_

2.)  $f(x) = 3^x ; (-1, 2]$



Domain: \_\_\_\_\_

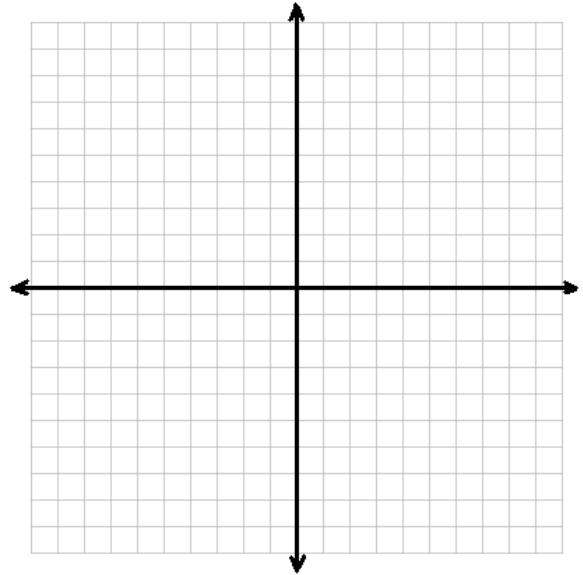
Range: \_\_\_\_\_



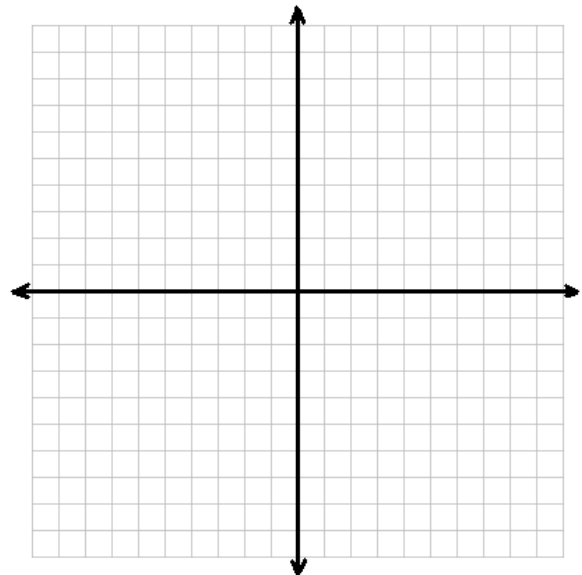
Name: \_\_\_\_\_

Graph the following equations.

1)  $f(x) = 3x - 2 ; [-2, 3]$



2)  $f(x) = -3x + 5 ; (-1, 4]$





Name: \_\_\_\_\_

Write each inequality in interval notation.

1.  $-3 < x < 4$

2.  $1 \leq x < 17$

3.  $6 \leq x \leq 7$

4.  $x > 2$

Write each interval as an inequality.

5.  $[5,8]$

6.  $(6,18]$

Write the set of integers represented by the inequality/interval.

7.  $(2,7]$

8.  $5 \leq x < 10$





Name: \_\_\_\_\_

Find the domain and range for the following:

1.)  $y = -2x - 7$

**(See 1A on notes for assistance)**

2.) Let,  $C(x) = 3x + 14$ , where  $C(x)$  stands for the number of calories burned while running  $x$  hours.

**(See 1B on notes for assistance)**

3.) Let  $M(x) = 50(4)^x$ , where  $M(x)$  stands for the population of mold that grows over  $x$  days.

**(See 1C on notes for assistance)**

4.) A parking garage charges \$1.25 for every hour a car is parked in their lot. The company always charges for the full hour. Find the domain and range over a 6 hour period.

**(See 4 on notes for assistance)**

Hours	Money Charged



Name: \_\_\_\_\_

Homework 63

Evaluate the following:  $f(x) = -2x - 7$  ,  $h(x) = x^2 - 2x + 1$

1)  $f(a - 2)$

2)  $h(-2)$

3)  $f(a + h) - f(a)$

4)  $h(a) - h(2)$



1. Which set of ordered pairs does *not* represent a function?
  - a)  $\{(3, -2), (-2, 3), (4, -1), (-1, 4)\}$
  - b)  $\{(3, -2), (3, -4), (4, -1), (4, -3)\}$
  - c)  $\{(3, -2), (4, -3), (5, -4), (6, -5)\}$
  - d)  $\{(3, -2), (5, -2), (4, -2), (-1, -2)\}$
  
2. Which relation is a function?
  - a)  $\left\{\left(\frac{3}{4}, 0\right), (0, 1), \left(\frac{3}{4}, 2\right)\right\}$
  - b)  $\left\{(-2, 2), \left(-\frac{1}{2}, 1\right), (-2, 4)\right\}$
  - c)  $\{(-1, 4), (0, 5), (0, 4)\}$
  - d)  $\{(2, 1), (4, 3), (6, 5)\}$
  
3. Given:  $\{(2, 1), (3, 6), (4, -3), (6, -11)\}$ , find the domain and range.

Evaluate the following functions for the given values. You must have work.

4. If  $f(x) = 3x - 4$ , find  $f(-2)$ .
5. If  $f(x) = -3x + 11$ , find  $f(2) + f(7)$
6. If  $f(x) = x^2 + 3x - 5$ , find the value of  $f(3)$ .



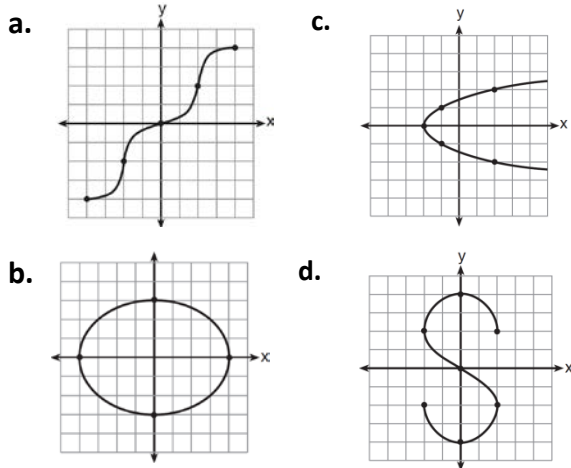
1) Which set of ordered pairs represents a function?

- a.  $\{(0,4), (2,4), (2,5)\}$
- b.  $\{(6,0), (5,0), (4,0)\}$
- c.  $\{(4,1), (6,2), (6,3), (5,0)\}$
- d.  $\{(0,4), (1,4), (0,5), (1,5)\}$

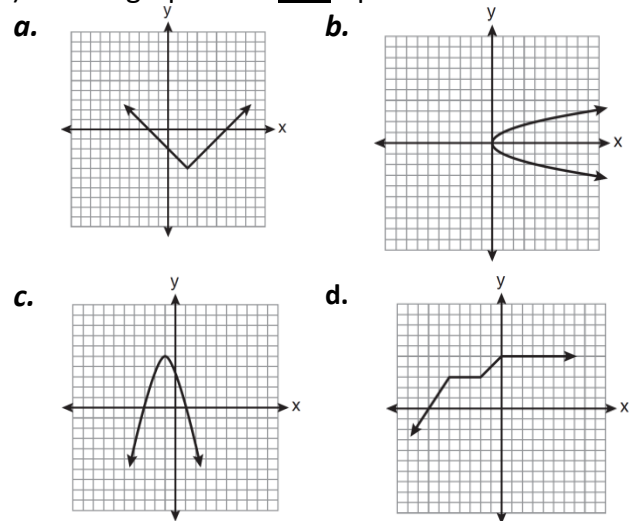
2) Which relation is *not* a function?

- a.  $\{(1,5), (2,6), (3,6), (4,7)\}$
- b.  $\{(4,7), (2,1), (-3,6), (3,4)\}$
- c.  $\{(-1,6), (1,3), (2,5), (1,7)\}$
- d.  $\{(-1,2), (0,5), (5,0), (2,-1)\}$

3) Which graph represents a function?



4) Which graph does not represent a function?



5) Given  $\{(2, 5), (3, 0), (6, 2), (4, 1)\}$   
Evaluate  $f(3)$

6) Given  $\{(2, 5), (3, 0), (6, 2), (4, 1)\}$   
What is  $x$  if  $f(x) = 2$ ?

